

# Micellization of Sliding Polymer Surfactants

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**ABSTRACT:** Following up a recent paper on grafted sliding polymer layers [*Macromolecules* 2005, 38, 1434–1441], we investigated the influence of the sliding degree of freedom on the self-assembly of sliding polymeric surfactants that can be obtained by complexation of polymers with cyclodextrins. In contrast to the micelles of quenched block copolymer surfactants, the free energy of micelles of sliding surfactants can exhibit two minima: the first corresponding to small micelles with symmetric arm lengths and the second corresponding to large micelles with asymmetric arm lengths. The relative sizes and concentrations of small and large micelles in the solution depend on the molecular parameters of the system. The appearance of small micelles drastically reduces the kinetic barrier, allowing for the fast formation of equilibrium micelles.

## 1. Introduction

Predicting, controlling, and finely tuning the self-assembly properties of amphiphiles through molecular design is a problem of central importance in physical chemistry.<sup>1,2</sup> It is arguably also one of its major contributions to other fields: in the biological realm, where self-assembled phospholipids build the walls of liposomes and cells; in cosmetics, pharmaceuticals, or detergency, where many formulations are self-assembled solutions of surfactants, phospholipids and other amphiphile molecules. In this context, diblock copolymers have emerged as a paradigm for self-assembly.<sup>3–6</sup> Typically, the insoluble block drives the chains to self-associate, and the compositional asymmetry between the soluble and insoluble blocks defines the assembling geometry.<sup>5</sup> The many possibilities for architecture building offered by polymer synthesis and the development of polymer theory led to an unprecedented power of molecular control over the self-assembling structures of these so-called macrosurfactants. It is nowadays possible, for instance, to build different self-assembled structures from diblock, triblocks, and many other block copolymers, to introduce charges at different places along the chains with single charge accuracy, to form reversible or frozen structures, to combine flexible and semi-flexible blocks, etc. However, a major difficulty still hinders progress in the predictive power of micellization theories. Indeed, the macromolecular character of such surfactants implies that there is a large kinetic barrier for micelle formation, and the thermodynamic predictions for typical quantities such as the critical micellar concentration or the aggregation number are in many cases only marginally relevant. In this paper we discuss a novel macrosurfactant architecture, based on rotaxane inclusion complexes,<sup>7</sup> that can lead to a significant decrease of the kinetic barrier to micellization.

Rotaxanes are molecular complexes formed when a ringlike molecule, the rotor, is threaded over a linear molecule, the rotating axis.<sup>7</sup> Unthreading of the ring can be prevented by subsequent capping of the axis ends.<sup>8,9</sup> Rotaxanes can be made by combining different linear polymers<sup>10,11</sup> with different cyclic

molecules, in several solvents.<sup>12</sup> One of the most well-studied systems involves poly(ethylene oxide) and  $\alpha$ -cyclodextrins (CD), which are oligosaccharides of six glucose units assembled as rings. Moreover, chemical conjugation of cyclodextrins with a hydrophobic tail leads to a novel type of surfactant<sup>13</sup> capable of integrating to a membrane or adsorb onto a surface. Surfactants of hydrophobically modified cyclodextrins can form micelles of rings.<sup>14</sup> When an inclusion complex formed by one  $\alpha$ -cyclodextrin and one PEO chain is attached to a surface by such surfactant or by chemical grafting the  $\alpha$ -CD, it results in a novel structure of polymer layers for which we recently<sup>15</sup> coined the acronym SGP layers, for sliding grafted polymer layers. Contrary to the usual end-grafted polymer layer, in the SGP layers the chains retain the ability to slide through the grafting ring, a new degree of freedom that allows, as we recently have shown, to better relax the layer structure. In particular, our work suggests that in spherical, starlike layers, as obtained for instance if one attaches the  $\alpha$ -CD ring to a small colloid, sliding of the polymers through the ring entails a truly versatile polymer layer structure. At low number of grafts the chains adopt mostly symmetric configurations with two comparable arm sizes whereas with many grafts the adopted configurations are asymmetric with essentially one long arm participating in the corona. It was also shown that there exists an intermediate range of grafting numbers where the number of arms participating in the corona is constant and where the addition of more grafts leads to the progressive replacement of symmetric configurations by twice as much asymmetric ones. Conversely, in flat dense SGP layers, chains adopt only asymmetric configurations, having hence the same structure as the quenched ones. An important consequence for self-assembly is that the free energy of the curved SGP layers has a different structure from the usual polymer layers grafted to spherical surfaces but that the free energy of flat SGP layers only marginally differs from their nonsliding equivalents. The ability of polymers to slide in the ring combined with the excluded-volume interactions disfavors some of the configurations of the chain. This feature of sliding polymers has some similarity with interaction driven reorganizations in living polymers such as for example the alignment induced growth in liquid crystals.<sup>16</sup>

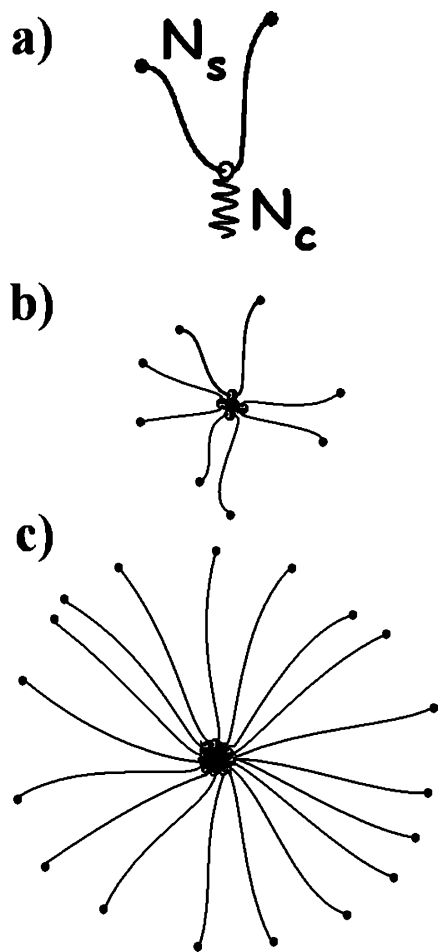
We consider the micellization of decorated “one-pearl necklaces” where the driving force for self-assembly is provided

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**Figure 1.** Schematic representation of (a) one sliding unimer comprised of soluble and insoluble blocks of lengths  $N_s$  and  $N_c$ , respectively, (b) a sliding small symmetric micelle, and (c) a sliding large asymmetric micelle.

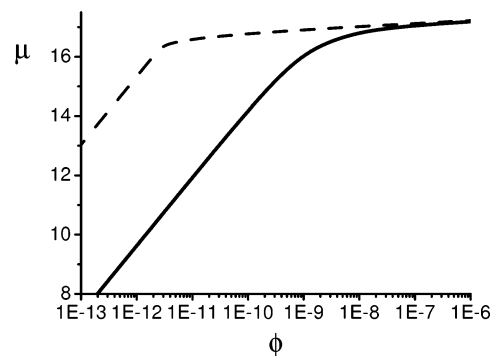
by the bead decoration, an insoluble chain chemically attached to the ring molecule (see Figure 1). The consequences of the sliding degree of freedom on the self-assembly of sliding polymeric surfactants are discussed by focusing on curved self-assembled structures, since for flat self-assembled layers only marginal differences are expected with the usual grafted layers. After a short reminder on diblock copolymer micellization, we recall the theoretical description of the spherical SGP layer, before discussing the possible micellization scenarios for this new family of macrosurfactant architectures (Figure 1).

## 2. Micellization of Diblock Copolymers

In this section we briefly discuss the theory of micellization of block copolymers (see e.g. ref 17). Consider a solution of monodisperse block copolymer with  $N_c$  insoluble and  $N_s$  soluble units. The insoluble blocks tend to aggregate and favor large aggregates while coronas of soluble blocks oppose the formation of large micelles. The free energy per unit volume,  $F$ , of the solution of noninteracting micelles is a sum running over the aggregation number  $p$ :

$$F = \sum_{p=1}^{\infty} c_p \left[ k_B T \ln \left( \frac{c_p}{e} N_T b^3 \right) + F_p \right] \quad (1)$$

where  $F_p$  and  $c_p$  is the free energy and the number density of a micelle comprising  $p$  surfactant chains, respectively. We assume that the Kuhn lengths of two blocks are equal between each



**Figure 2.** Chemical potential  $\mu$  as a function of the total concentration for quenched (dashed line) and sliding (solid line) micelles. Parameters used are:  $N_s = 300$ ,  $N_c = 62$ , and  $\sigma = 0.5$ .

other and equal to the solvent size  $b$ . Thus, the multiplier  $N_T b^3$  with  $N_T = N_c + N_s$  being the total volume of a copolymer.<sup>18</sup> This multiplier was often overlooked; a general discussion is provided by Riess,<sup>19</sup> who gives the relevant elementary volume, in our case  $N_T b^3$ , for microemulsions, assemblies of droplets, etc.

The equilibrium distribution of chains in micelles is obtained by minimizing  $F$  with respect to  $c_p$  along with the mass conservation constraint

$$\sum_{p=1}^{\infty} p c_p = \phi \quad (2)$$

where  $\phi$  is the total number of chains per unit volume. This gives the equilibrium densities of  $p$ -arm micelles in the form  $c_p N_T b^3 = \exp\{(\mu p - F_p)/k_B T\}$ , where

$$\mu = F_1 + k_B T \ln(c_1 N_T b^3) \quad (3)$$

is the chemical potential of unimers.

Thus, we can rewrite the equilibrium  $c_p$  as

$$c_p = \frac{(c_1 N_T b^3)^p}{N_T b^3} \exp\left(-\frac{F_p - p F_1}{k_B T}\right) \quad (4)$$

Rather than the distribution  $c_p$ , we will often use the more convenient function  $\Omega_p = \ln(c_p/c_p)$ :

$$\Omega_p = F_p - p F_1 - (p - 1) k_B T \ln(c_1 N_T b^3) \quad (5)$$

which may be considered as the thermodynamic potential. Given a value of  $c_1$  in eq 4, we can calculate the whole distribution  $c_p$  and the corresponding total chain concentration  $\phi$ . Experimentally, the chemical potential  $\mu$  is often studied as a function of  $\phi$ . We obtained the chemical potential curve from eqs 2–4 with  $c_1$  as the parameter. A kink in the representation (Figure 2, dashed line) is commonly used as an indicator for the onset of micellization. Usually only a narrow range of unimer concentrations at equilibrium  $c_1$  falls in the physically acceptable condition:  $N_T \phi b^3 \ll 1$ . When no interaction between micelles is accounted for, the more stringent criterion  $\sum_p c_p V_p < 1$  should be obeyed where  $V_p$  is the volume of a micelle comprising  $p$  surfactants.

The micellization scenario depends on the precise form of the free energy  $F_p$ , discussed in the following paragraphs for quenched copolymers and annealed sliding copolymers.

## 3. Free Energy of Starlike Micelles

The free energy of a micelle contains the molecular characteristics of the micellization process. Thus, to investigate the

micellization of sliding polymer surfactants, we have to specify the explicit form of the corresponding  $F_p$ . The free energy of a micelle is the sum of the core and of the corona contributions. Hereafter energies are expressed in  $k_B T$  units.

**3.1. Core Contribution.** We assume that the insoluble blocks form a dense homogeneous core where soluble blocks and the solvent cannot penetrate. Hence, the micelle free energy has two core contributions: (i) the surface tension term,  $F_c = 4\pi\sigma R_c^2$ , where  $R_c$  is the radius of the core and  $\sigma$  is the core-solvent surface tension expressed in  $k_B T/b^2$  units. For an incompressible core of size  $R_c = (3/(4\pi)pN_c)^{1/3}b$ , this leads to  $F_c = c\sigma N_c^{2/3}p^{2/3}$ , where  $c = (36\pi)^{1/3}$ . (ii) Gaussian elastic contributions arising from stretching of the insoluble blocks in the core,  $F_{el} = wpR_c^2/(N_c b^2) = wp^{5/3}/N_c^{1/3}$ , where  $w = 3\pi^2/80$  reflects the spherical geometry of the core. The value of  $w$  is obtained from a self-consistent field (SCF) theory in the strong stretching limit.<sup>20</sup> Although the elastic contribution of the core is only larger than  $k_B T$  for micelles with large cores, we keep it for convenience.<sup>21</sup>

**3.2. Corona Contribution.** For large soluble blocks, as considered here, the corona is usually envisioned as a star of soluble blocks radially stretched away from the spherical core. The partition function  $Z_p$  of a star with  $p$  equal arms of contour length  $N_s$  is given by the critical exponent  $\gamma_p$ ,  $Z_p \sim N_s^{\gamma_p-1}$ .<sup>22</sup> Star exponents  $\gamma_p$  are known exactly in two dimensions and for ideal chains ( $d \geq 4$ ). In three dimensions  $\epsilon$  expansions ( $\epsilon = 4 - d$ ) are available, to first order:<sup>22</sup>

$$\gamma_p - 1 = -\frac{\epsilon}{16}p(p-3) + o(\epsilon^2) \quad (6)$$

Recently, Monte Carlo simulations were carried out by Hsu et al.<sup>23</sup> in order to find the exact values of  $\gamma_p$  for a large range of  $p$  values. The results do not quantitatively agree with the classical predictions of the Daoud-Cotton model<sup>24</sup>  $\gamma_p - 1 \sim -p^{3/2} + \dots$ , indicating that the asymptotic limit of very large  $p$  numbers, where subdominant powers of  $p$  are negligible, is not yet reached. If we insist on fitting Hsu et al.'s results to the Daoud and Cotton model, say between  $p = 20$  and  $p = 60$ , where the simulated arms are still fairly long, the obtained amplitude is close to 0.2. It seems that the asymptotic limit, restricted to the leading term, is also out of experimental reach. The authors showed that the best fit of the simulation data with a power law  $\sim -p^z$  is obtained with  $z = 1.68$ . Our discussion below is based on the simulation data, and we will use, for convenience, the fitting function of the form close to eq 6:  $-p(Bp - A)^z/16$  reflecting the simulation results. The best fit is

$$\gamma_p - 1 = -\frac{p}{16}(1.5p - 6)^{0.7}, \quad p > 4 \quad (7)$$

while for  $p < 4$  we take values from the table of ref 23.

When there is a sliding degree of freedom, the free energy of the corona has a more complex structure. The possibility for the soluble blocks to slide through a ring results in an annealed arm length distribution in the coronas of such micelles made of  $p$ -chains. Adjusting the length of the arm in the corona can decrease the crowding effect originating from the steric repulsions between soluble blocks. In our previous paper,<sup>15</sup> we found three possible regimes for the sliding coronas depending on the number of sliding chains per aggregate. The transition between these regimes is determined from a threshold value of the number of arms  $p^*$ , defined by the conditions  $\gamma_{p^*} - \gamma_{p^*-1} > -1$  and  $\gamma_{p^*+1} - \gamma_{p^*} \leq -1$ . If the number of chains per aggregate

is small,  $p \leq p^*/2$ , the corona is fully annealed, and the sliding chains are likely to adopt any configuration. We call such micelles symmetric micelles, since symmetric configurations are prevalent. The corona properties are determined by configurations with  $2p$  arms, and its partition function is given by<sup>15</sup>

$$Z_p \propto N_s^p N_s^{\gamma_{2p}-1}, \quad p \leq p^*/2 \quad (8)$$

For a larger number of grafting chains, in the intermediate regime,  $p^*/2 < p < p^*$ , only  $p^* - p$  chains adopt symmetric configurations, while the rest of the chains are stretched out from the ring. The corona has  $p^*$  arms, and its partition function reads

$$Z_p \propto N_s^{p^*-p} N_s^{\gamma_{p^*}-1}, \quad p^*/2 < p < p^* \quad (9)$$

For even larger micelles,  $p \geq p^*$ , all the chains in the corona are strongly asymmetric, and the partition function of the corona coincides with the partition function of a quenched star:

$$Z_p \propto N_s^{\gamma_p-1}, \quad p \geq p^* \quad (10)$$

The determination of the threshold value of the number of arms  $p^*$  strongly depends on our knowledge of the values of the critical exponents  $\gamma_p$ . Our previous estimates<sup>15</sup> were based on the first-order  $\epsilon$  expansion (eq 5), yielding  $p^* = 9$ . However, if we use the values obtained from the computer simulations in ref 23, we get  $p^* = 18$ . Thus, in the following we assume the latter estimate as most accurate. We use our fitting function (6) for the values of  $\gamma_p$ , and the free energy of the sliding corona of a micelle  $F_p^{\text{corona}} = -\ln Z_p$  is determined as a piecewise function of the number of chains  $p$ .

**3.3. Total Free Energy.** Combining all terms together, the energy of a micelle is given by

$$F_p = F_p^{\text{corona}} + c\sigma N_c^{2/3}p^{2/3} + wp^{5/3}/N_c^{1/3} \quad (11)$$

with

$$F_p^{\text{corona}} = f(p) \ln N_s \quad (12)$$

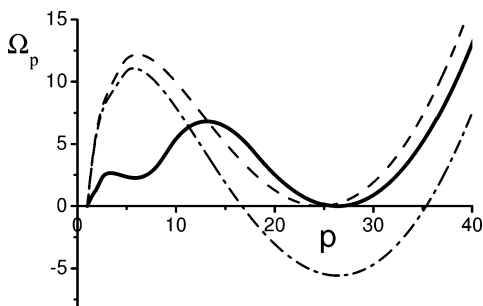
where  $f(p)$  is defined piecewise by eqs 8–10 as discussed in the previous section for sliding copolymers whereas for quenched copolymers:  $f(p) = -(\gamma_p - 1)$ . This free energy neglects contributions arising from the shielding of the solvophobic chains from the contact with the solvent as well as these stemming from the extensive part of the corona. They are both proportional to the aggregation number  $p$  and hence can be absorbed in the chemical potential  $\mu$  (eq 3).

Note that the corona free energy of sliding surfactant unimers ( $p = 1$ ) is  $F_1^s = -\gamma_1 \ln N_s$  while that of the quenched unimer is  $F_1^q = -(\gamma_1 - 1) \ln N_s$ . Thus, the free energy of sliding surfactant is about  $-\ln N_s$  less than that of quenched ones with the same soluble block size.

Next we use the expressions of the free energy  $F_p$  to compute the micelle size distribution for both quenched and sliding copolymers.

#### 4. Micelle Size Distribution: Sliding vs Quenched Copolymers

A preferred aggregation number is reflected by a minimum in the potential  $\Omega_p$ . Roughly speaking, the corresponding aggregates will dominate over unimers if the minimum potential value is negative. For usual quenched copolymers the potential has only one, rather sharp, minimum (see Figure 3), and the polydispersity of spherical micelles is usually very low, the



**Figure 3.** Potential  $\Omega_p = \ln(c_1/c_p)$  as a function of the aggregation number  $p$  for sliding micelles (solid line, total surfactant concentration  $\phi = 3 \times 10^{-8}$ ) and for quenched micelles (dashed line,  $\phi = 1 \times 10^{-10}$ , dash-dotted line,  $\phi = 3 \times 10^{-8}$ , same as for sliding micelles) for the set of parameters:  $N_s = 300$ ,  $N_c = 70$ , and  $\sigma = 0.5$ . Micelles form almost without kinetic barrier from sliding polymer surfactants.

distribution  $c_p$  being sharply peaked around the average aggregation number  $p_m$ . In this sense, quenched copolymer association should be termed *closed* association where the distribution is dominated by aggregates of uniform size with weak fluctuations appearing at a well-defined unimer concentration. In the common used classification, *open* association means that aggregates of different sizes significantly contribute to the distribution and appear gradually. The practical relevance of this classification has been critically discussed recently.<sup>25</sup>

The average aggregation number and the cmc are found from the conditions  $\Omega_p = \partial\Omega_p/\partial p = 0$ .<sup>26</sup> The minimum is separated from the origin by a kinetic barrier. Thus, it takes a typical time  $\sim \exp(U_{\max}/k_B T)$  for isolated chains to form a micelle, with  $U_{\max}$  the maximum of the barrier. A rough scaling estimate gives  $U_{\max}/k_B T \sim \sigma N_c^{6/5}$ .<sup>27</sup> Depending on the conditions, this time for usual block copolymer micelles can be very large. Very often, quenched copolymer micelles do not form over reasonable time scales at the cmc, where they are thermodynamically favored. Only at much higher concentrations, the barrier  $U_{\max}/k_B T$  becomes low (see Figure 3).

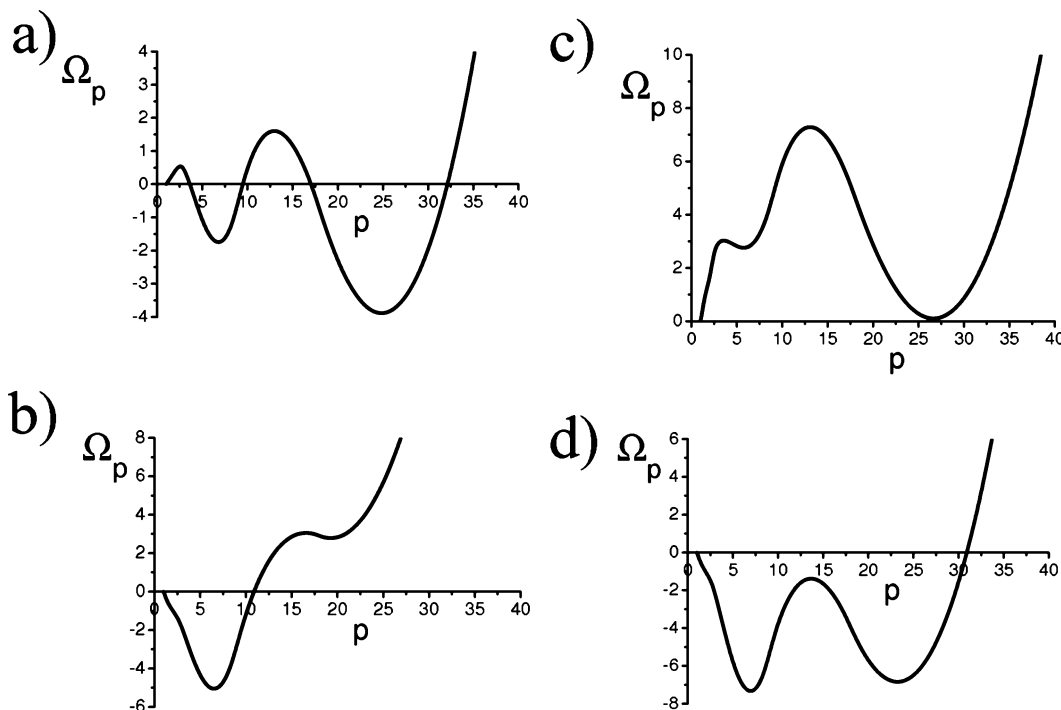
In contrast to the quenched case, the potential  $\Omega_p = \ln(c_1/c_p)$  (eq 5) for sliding micelles can have two minima. One corresponds to small symmetric micelles with aggregation numbers up to 9, and the second corresponds to large asymmetric micelles (Figure 3). The appearance of small micelles leads to a drastic decrease of the kinetic barrier, such that the first minimum is separated from the origin by a barrier of order  $k_B T$ , leading to the fast formation of equilibrium micelles. The chemical potential  $\mu$  of sliding copolymers as a function of  $\phi$  presents a rounded kink as compared to the quenched case (Figure 2).

Depending on molecular parameters of the system, the formation of small micelles can follow (Figure 4a,c) or precede (Figure 4b,d) the formation of large micelles. Typical examples of the mass distribution in micelles,  $p c_p/\phi$ , with increasing polymer concentration are shown in Figure 5. The equilibrium aggregation number switches between symmetric (small) and asymmetric (large) micelles as the concentration increases. Tuning the parameters of the system, either the surface tension of the core,  $\sigma$ , or the relative length of the blocks (in our case we vary  $N_c$  keeping  $N_s$  constant), we can change the order of the appearance of small and large micelles. Figure 6 shows the corresponding state diagram which is related to Figure 7. When large and small micelles coexist, the large ones usually dominate by mass. Hence, we represent the boundary between large and large plus small micelles by a dashed line.

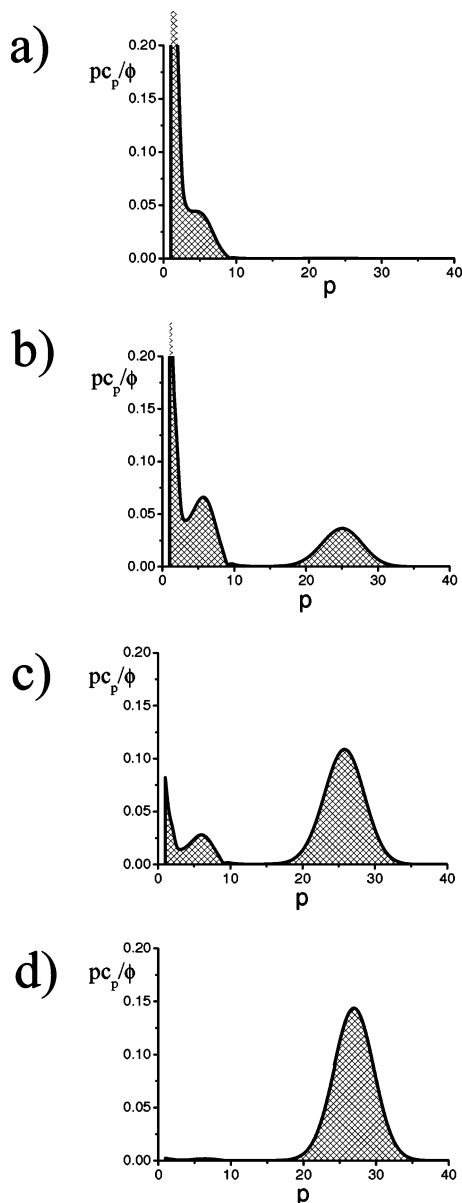
Though the full potential (eq 5) is uneasy to handle analytically, we may somewhat simplify it by omitting the stretching of the insoluble blocks. The aggregation number of a vanishing minimum of this approximate potential (for some chemical potential) is then solution of the following equation:

$$\frac{(p-1)\frac{\partial f(p)}{\partial p} - f(p) + f(1)}{p^{2/3} + 2p^{-1/3} - 3} = \frac{1}{3} \frac{c\sigma N_c^{2/3}}{\ln N_s} \quad (13)$$

The left-hand side of this equation  $h(p)$  collects all the terms



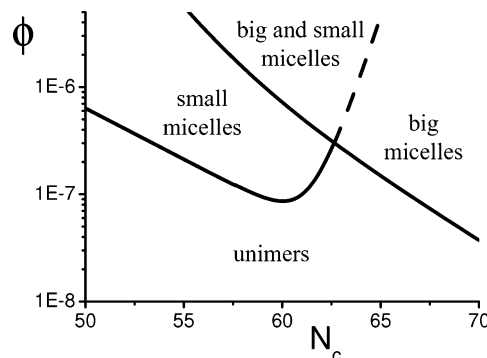
**Figure 4.** Typical examples of the potential  $\Omega_p = \ln(c_1/c_p)$  for a different set of parameters. (a) Large micelles appear first:  $N_s = 300$ ,  $N_c = 60$ ,  $\sigma = 0.5$ ,  $\phi = 3.3 \times 10^{-5}$ . (b) Small micelles appear first:  $N_s = 300$ ,  $N_c = 55$ ,  $\sigma = 0.6$ ,  $\phi = 2.0 \times 10^{-8}$ . (c) Large micelles dominate:  $N_s = 1000$ ,  $N_c = 60$ ,  $\sigma = 0.5$ ,  $\phi = 2.8 \times 10^{-5}$ . (d) The depth of the two minima is of the same order:  $N_s = 10\,000$ ,  $N_c = 60$ ,  $\sigma = 0.7$ ,  $\phi = 7.8 \times 10^{-7}$ .



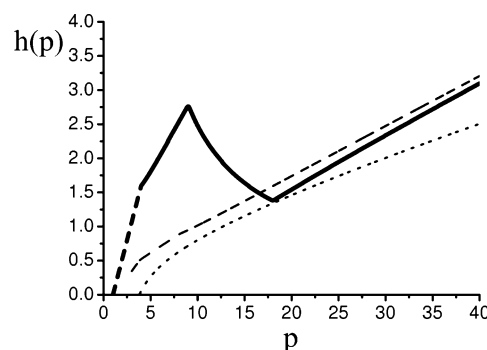
**Figure 5.** Evolution of the mass distribution in micelles,  $pC_p/\phi$ , with increasing total concentration  $\phi$ : (a)  $2 \times 10^{-10}$ , (b)  $5 \times 10^{-10}$ , (c)  $2 \times 10^{-9}$ , and (d)  $8 \times 10^{-8}$  for  $N_s = 300$ ,  $N_c = 70$ , and  $\sigma = 0.5$ . Free unimers first transform in small micelles, and then the large micelles appear and consume the most of the unimers.

depending on  $p$ . Thus, in this approximation the desired aggregation numbers depend only on the combination of parameters  $\beta = \frac{1}{3}c\sigma N_c^{2/3}/\ln N_s$ . It is easy to see that in the quenched copolymer case there is indeed only one solution of  $p_m$  and in the Daoud–Cotton limit  $p_m \sim (\sigma N_c^{2/3}/\ln N_s)^{6/5}$ , a classical result.

It is worthwhile discussing the number of solutions of eq 13 as a function of the parameter  $\beta$  for sliding copolymers. It can be obtained by counting the number of intersections of  $h(p)$  (Figure 7) with the line parallel to the abscissa. In the first region,  $\beta \lesssim 1.38$ , there is only one intersection. It corresponds to one minimum in  $\Omega_p(p)$ . The number of arms  $p$  is small; thus, this region corresponds to the coexistence of unimers with small symmetric micelles. In the region  $1.38 \lesssim \beta \lesssim 2.77$  there are three intersections showing the existence of two minima separated by a barrier. Small micelles with aggregation numbers  $p < p^*/2 = 9$  coexist with large micelles with  $p > p^* = 18$ . In the third regime,  $\beta \gtrsim 2.77$ , there are only asymmetric micelles of high aggregation numbers. The crossover values of the



**Figure 6.** Schematic diagram of different types of micelles present in a solution. Labels designate regions where the indicated structures are dominant. Parameters used:  $N_s = 300$ ,  $\sigma = 0.5$ . The boundary between the region of big micelles and the region of the coexistence of small and big micelles is indicated by dashed line because big micelles usually dominate by mass in both regions.



**Figure 7.** Graphical solution of eq 12. For values of  $\beta = \frac{1}{3}c\sigma N_c^{2/3}/\ln N_s$  between 1.38 and 2.77 a small symmetric micelle and a large asymmetric one can be more stable with respect to the unimer (for different chemical potentials). The bold dashed line ( $p < 3$ ) was not calculated. The thin dashed line corresponds to quenched copolymers, where there is only one micelle size. The dotted line corresponds to the Daoud–Cotton model for quenched copolymers.

parameter  $\beta$  are compatible with Figure 6, where the crossover values of  $N_c$  are 40 and 93. For given values of parameters ( $N_c$ ,  $N_s$ ,  $\sigma$ ) it should further be checked that the micelles exist for physical concentrations.

Figure 7 also shows the aggregation number of quenched copolymer micelles as a function of  $\beta$  (dashed line); the difference with large sliding micelles is due to a shift in the free energy of a unimer from  $F_1^s$  to  $F_1^q$ . The Daoud–Cotton line is also shown (dotted line). As already discussed, no agreement can be obtained using a simple Daoud–Cotton power law.

## 5. Concluding Remarks

Sliding diblock copolymer surfactants where the soluble and insoluble blocks are topologically tethered by a small ring show a much richer micellization behavior than the corresponding quenched diblock copolymers. When the size of the insoluble blocks is not too long, both small micelles (with an aggregation number slightly smaller than  $p^*/2 = 9$ ) and large micelles (with an aggregation number slightly larger than  $p^* = 18$ ) may coexist in the solution. In the small micelle each copolymer participates in the corona with two arms whereas in the large micelle the asymmetric arm length distribution is dominant. Hence, coronas in small and large micelles comprise a similar number of arms. Small micelles can form without appreciable kinetic barrier at the lowest concentration where they are thermodynamically favored. The barrier opposing the formation of the larger micelle remains modest. This is in marked contrast with the corre-

sponding quenched copolymers where kinetic barriers are very high at the same concentrations. Which micelle appears first with increasing concentration depends on the block asymmetry. At somewhat higher concentrations, the micelle size distribution broadens and covers the whole range from the small to the large aggregation number described previously.

For large insoluble blocks only the large micelles, similar to the quenched ones, form. Because of the loss of the sliding degree of freedom upon association, the annealed cmc is higher than the quenched one. On the other hand, the kinetic barrier is markedly lower for annealed copolymer micelles (typically by a factor 2) that may form at the cmc within experimental times.

Our description of starlike micelles is based on excellent values of the vertex exponents from a recent simulation by Hsu et. al.<sup>23</sup> We think that this improves over the standard Daoud and Cotton model for the classic quenched micelles.

Sliding copolymers are a new interesting example of nonionic annealed copolymers. Some charged micelles can also display a similar behavior as reported by Zhulina and Borisov for insoluble/annealed-polyelectrolyte diblocks.<sup>28</sup> To our knowledge, only flat brushes of complexing polymers have been studied theoretically.<sup>29</sup> Diblocks where the soluble block forms a complex with small colloids (proteins) also belong to the class of annealed copolymers. One may speculate whether such diblocks also form two types of micelles.

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